ANN ARBOR — What part of math success comes from knowing fractions? More than you might think, according to a new study that analyzed long-term data on more than 4,000 children from both the United States and the United Kingdom.

Published in the current issue of the peer-reviewed journal Psychological Science, the study found that understanding fractions and division at age 10 predicted algebra and overall math achievement in high school, even after statistically controlling for a wide range of factors including parents’ education and income, and children’s age, gender, I.Q., reading comprehension, working memory, and knowledge of whole number addition, subtraction and multiplication.

“These findings demonstrate an immediate need to improve the teaching and learning of fractions and division,” said University of Michigan researcher Pamela Davis-Kean, a co-author of the study and director of the Center for the Analysis of Pathways from Childhood to Adulthood at the U-M Institute for Social Research.

“We suspected that early knowledge in these areas was absolutely crucial to later learning of more advanced mathematics, but did not have any evidence until now,” said Robert Siegler, a cognitive psychologist at Carnegie Mellon University and the lead author of the study.

“The clear message is that we need to improve instruction in long division and fractions, which will require helping teachers to gain a deeper understanding of the concepts that underlie these mathematical operations. At present, many teachers lack this understanding. Because mastery of
fractions, ratios and proportions is necessary in a high percentage of contemporary occupations, we need to start making these improvements now.

From factory workers to Wall Street bankers, a reasonable proficiency in math is a crucial requirement for most well-paying jobs in a modern economy. Yet, over the past 30 years, mathematics achievement of U.S. high school students has remained stagnant — and significantly behind many other countries, including China, Japan, Finland, the Netherlands and Canada.

The current study identifies a major source of the gap — U. S. students’ inadequate knowledge of fractions and division. Although fractions and division are taught in elementary school, even many college students have poor knowledge of them.

The research was supported by a grant to the Center for the Analysis of Pathways from Childhood Adulthood by the National Science Foundation.

A team of eight investigators conducted the analyses: Davis-Kean, Siegler, Greg Duncan of the University of California-Irvine, UM’s Maria Ines Susperreguy and Meichu Chen, Kathryn Duckworth of the University of London, the University of Chicago’s Amy Claessens and Vanderbilt University’s Mimi Engel.

For the study, the team examined two nationally representative datasets, one from the U.K. and one from the U.S. — the Panel Study of Income Dynamics, conducted at the U-M Institute for Social Research since 1968. The data from the Panel Study of Income Dynamics included 599 children who were tested in 1997 as 10-to-12-year-olds and again in 2002 as 15-to-17-year-olds. The data from the U.K. included 3,677 children who were tested in 1980 as 10-year-olds and in 1986 as 16-year-olds. The importance of fractions and division for long-term mathematics learning was evident in both data sets, despite the data being collected in two different countries almost 20 years apart.

“This research is a good demonstration of what collaborations between psychologists, economists, public policy analysts and education scientists can create,” said Davis-Kean, who is an associate professor of psychology at the UM College of Literature, Science and the Arts and an associate research professor at ISR. “Instead of relying on results from a single study, this study replicates findings across two national data sets in two different countries, which strengthens our confidence in the results.”